

Algorithms and Uncertainty

Summer Term 2021

Exercise Set 9

Exercise 1:

(5 Points)

State a no-regret algorithm for the case that $\ell_i^{(t)} \in [-\rho, \rho]$ for all i and t . Also give a bound for the regret. You should reuse algorithms and results from the lectures.

Exercise 2:

(5 Points)

We consider a different form of feedback. After step t , the algorithm does not get to know $\ell_i^{(t)}$ for all i but a noisy version. More precisely, an adversary first fixes the sequence $\ell^{(1)}, \dots, \ell^{(T)}$, where all costs are in $[0, 1]$. Afterwards, from this sequence $\bar{\ell}^{(1)}, \dots, \bar{\ell}^{(T)}$ is computed, where $\bar{\ell}_i^{(t)} = \ell_i^{(t)} + \nu_i^{(t)}$ and $\nu_i^{(t)}$ is an independent random variable on $[-\epsilon, \epsilon]$ with $\mathbf{E}[\nu_i^{(t)}] = 0$. State a no-regret algorithm and a bound for the regret. You can make use of the previous exercise and the ideas presented in lecture 20.

Exercise 3:

(3 Points)

In the lecture, we used that $\mathbf{E} \left[\min_i \sum_{t=1}^T \ell_i^{(t)} \right] \leq \min_i \mathbf{E} \left[\sum_{t=1}^T \ell_i^{(t)} \right]$ or $\mathbf{E} \left[\max_i \sum_{t=1}^T r_i^{(t)} \right] \geq \max_i \mathbf{E} \left[\sum_{t=1}^T r_i^{(t)} \right]$ respectively. Give a proof of this inequality.