

## Algorithms and Uncertainty

Winter Term 2025/26

Tutorial Session - Week 13

### Exercise 1:

Show that the EXP3 algorithm can also be applied to an instance of Stochastic Multi-Armed Bandits from lecture 17.

Additionally, show that, when setting  $\eta = \sqrt{\frac{\ln n}{nT}}$  and  $\gamma = n\eta$ , this leads to an expected regret of at most  $3\sqrt{nT \ln n}$ .

**Hint:** You can use the bound on the external regret of EXP3 from lecture 20.

### Exercise 2:

For the normed vector space  $(\mathbb{R}^d, \|\cdot\|)$ , the unit ball with respect to  $\|\cdot\|$  is defined as the set  $\{x \in \mathbb{R}^d : \|x\| \leq 1\}$ .

- (a) Show that the unit ball with respect to the 1-norm is convex.
- (b) Show that the unit ball with respect to the 2-norm is convex.
- (c) Show that the unit ball with respect to the  $\infty$ -norm is convex.
- (d) Does the same result hold for an arbitrary  $p$ -norm with  $p > 1$ ? What about  $p < 1$ ?